Improved Molecular Constants of Acetylene Obtained from the v_5 Band System

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A vibration-rotation band system of acetylene of the Π_u bending vibration v_5 has been recorded with high resolution by a Bruker IFS 120 HR Michelson spectrometer. From the analysis of the hot band of the normal isotopic species, $v_4 + v_5 - v_4$, and the fundamental band of HC¹³CH in natural abundance an improved set of constants has been derived. The intensity perturbation due to the l-type resonance has been clearly observed in the band system $v_4 + v_5 - v_4$.

I. Introduction

There exists a number of excellent spectroscopic papers concerning the vibration-rotation spectra of acetylene. Because of its large rotational constant, the spectra of this molecule were fairly well analyzed by Rao and coworkers [1], and Plíva and coworkers [2] using a large grating spectrometer. Recent improvement in the analysis was made by Hietanen and Kauppinen [3], who used their Michelson-type Fourier transform spectrometer.

In the present study we have remeasured the v_5 band of acetylene using the Gießen Fourier transform spectrometer in order to support our diode laser spectroscopic work near the 700 cm⁻¹ wave number region. In this frequency region the acetylene spectrum is rich and thus provides densely spaced calibration points. Several reasons stimulated the analysis of some bands in this spectrum resulting in an improved set of molecular constants: (i) the intrinsically beautiful and textbook like spectra warrant a closer investigation in their own right. As an example we compare in Fig. 1 the FT spectrum of the HC13CH Q-branch near 728 cm⁻¹ with the cooled jet diode laser spectrum; (ii) recent supersonic jet spectroscopy shows that several interesting Van-der-Waals complexes can be formed with acetylene [4, 5] and (iii) acetylene is an interstellar molecule which is supposed to play an

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important role in the interstellar chemistry and can only be observed via its IR spectra [6].

This paper reports the spectrum and analysis of the hot band $\nu_4 + \nu_5 - \nu_4$ of the main species and of the ν_5 band of HC¹³CH. The high resolution Fourier transform spectrum supplies not only the usual large number of line positions but also gives fairly accurate line intensities of the transitions. In the present study we have used the latter FT property to discuss the intensity perturbation due to the *l*-type resonance.

II. Experimental Procedure and Observed Spectrum

The spectrum was recorded with a Bruker IFS 120 HR vacuum Michelson-type interferometer in Gießen [7]. Using a 17 cm long cell we have measured the spectrum at a pressure of about 85 Pa at room temperature and with a resolution of 0.0036 cm⁻¹. The line positions were calibrated by using CO₂ lines as the wavenumber standard [8]. The recording of the spectrum spans from 410 to 970 cm⁻¹; we covered such a large frequency region in order to use the spectrum to calibrate our diode laser spectrometers. In the present paper we report only on the analysis of a small portion of the observed spectrum. One Q-branch structure is reproduced in Fig. 2 to demonstrate the quality of the spectrum. Industry grade acetylene was used as the sample gas without further purification.

Although the *B* rotational constant of this molecule is very large, about 35 GHz, the observed absorption lines are fairly densely populated due to the excitation

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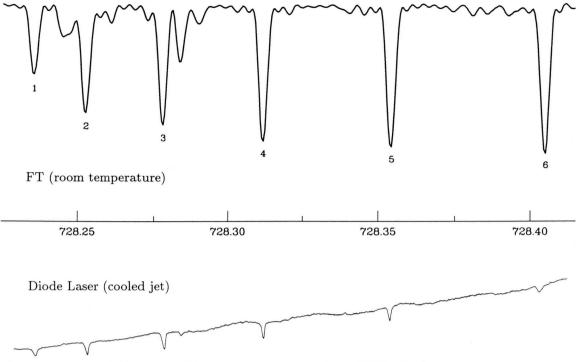


Fig. 1. Comparison of FT and cooled jet diode laser spectrum of the $HC^{13}CH$ (0, 1^{1} –(0, 0) Q-branch. As expected, no intensity alternation is observed for adjacent J-lines.

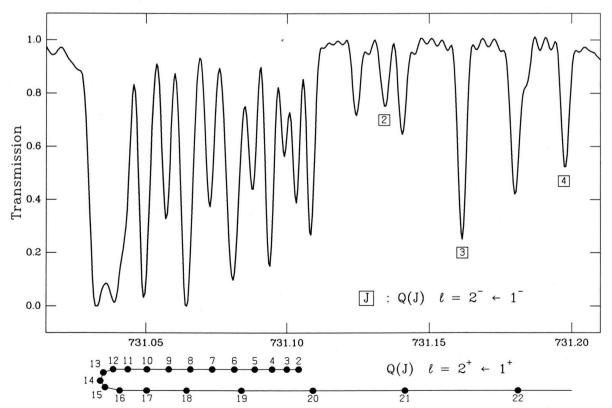


Fig. 2. A portion of the observed spectrum showing the Q-branch region of the $(1, 1)^2 - (1, 0)^1$ band near 731.1 cm⁻¹. The spectrum of the symmetric species shows the 3:1 intensity alternation caused by the hydrogen nuclear spin.

of many hot and isotope bands. Among them we have analyzed the hot band from the Π_g bending vibration $v_4=1$ state, i.e. the hot band $v_4+v_5-v_4$, because the Π_g bending vibration is infrared inactive and this band is one of the limited sources of information of the $v_4=1$ state. In addition we have analyzed the v_5 band of HC¹³CH. We apply the numbering of the normal modes of the symmetric species for this asymmetrical molecule as well, although the center of symmetry is missing as a means to distinguish Π_g and Π_u species.

The assignments of the hot band $v_4 + v_5 - v_4$ of the normal species and the fundamental v_5 band of $HC^{13}CH$ were straight forward because the constants available from the literature [3] are good enough to predict the line positions. In addition we could proof the assignments by comparing the FT spectra at room temperature with the diode laser supersonic jet spectra for which the spectra are much simpler because of the low temperature.

III. Analysis

The observed line positions are analyzed by using an effective Hamiltonian of Yamada, Birss, and Aliev [9] for the vibrational states (v_4, v_5)

$$\hat{H} = \hat{h}_{\mathrm{d}} + \hat{h}_{\mathrm{0}} + \hat{h}_{\mathrm{2}} \tag{1}$$

with

$$\hat{h}_{d} = G_{v} + x_{L44} \, \hat{p}_{z(4)}^{2} + x_{L45} \, \hat{p}_{z(4)} \, \hat{p}_{z(5)} + x_{L55} \, \hat{p}_{z(5)}^{2}$$

$$+ \left\{ B_{v} + d_{JL} \, \hat{J}_{z}^{2} \right\} (\hat{J}^{2} - \hat{J}_{z}^{2}) - D_{v} (\hat{J}^{2} - \hat{J}_{z}^{2})^{2}$$

$$+ H_{v} (\hat{J}^{2} - \hat{J}_{z}^{2})^{3}, \qquad (2)$$

$$\hat{h}_{0} = (r_{45} + r_{J45} \, \hat{J}^{2} + r_{JJ45} \, \hat{J}^{4})$$

$$\cdot (\hat{L}_{++(4)} \, \hat{L}_{--(5)} + \hat{L}_{--(4)} \, \hat{L}_{++(5)}), \qquad (3)$$

$$\hat{h}_{2} = \frac{1}{2} \left\{ \hat{L}_{++(4)} \hat{J}_{-}(q_{4} + q_{J4} \hat{J}^{2} + q_{JJ4} \hat{J}^{4}) \hat{J}_{-} + \hat{L}_{--(4)} \hat{J}_{+}(q_{4} + q_{J4} \hat{J}^{2} + q_{JJ4} \hat{J}^{4}) \hat{J}_{+} \right\}$$

$$+ \frac{1}{2} \left\{ \hat{L}_{++(5)} \hat{J}_{-}(q_{5} + q_{J5} \hat{J}^{2} + q_{JJ5} \hat{J}^{4}) \hat{J}_{-} + \hat{L}_{--(5)} \hat{J}_{+}(q_{5} + q_{J5} \hat{J}^{2} + q_{JJ5} \hat{J}^{4}) \hat{J}_{-} \right\}. (4)$$

The operator $\hat{h}_{\rm d}$ is diagonal with the vibrational energy $G_{\rm v}$, the anharmonicity constants x_{Lij} , the effective rotational constants $B_{\rm v}$, the centrifugal distortion constants $D_{\rm v}$ and $H_{\rm v}$, and the l-dependence constant d_{JL} . The operator \hat{h}_0 represents the vibrational l-doubling, where r_{45} is the doubling constant, and r_{J45} and

 r_{JJ45} are its J dependences. The operator \hat{h}_2 represents the rotational l-doubling, where q_4 and q_5 are the l-type doubling constants; q_{J4}, q_{J5}, q_{JJ4} , and q_{JJ5} are their J dependences. The notation here is slightly different from those of [9]; we have reversed the order of the suffices for some constants.

In the present paper, the vibrational states are distinguished by the notation (v_4, v_5) . When the l-substates have to be distinguished, we use the notation $(v_4, v_5)^{lt}$, where l is the total vibrational angular momentum $(l_4 + l_5)$, and t indicates + or - in Wang's combination. The corresponding wavefunctions are given by $|v_4, v_5|$; $|t\rangle$. These notations are the same as used for HCCCN and DCCCN by Yamada and coworkers [10, 11]. We repeat here the most important definitions: Wang's linear combinations used in the present study are

$$\begin{aligned} |0,1;1^{\pm}\rangle &= \{|0^{0},1^{1};J,1\rangle \pm |0^{0},1^{-1};J,-1\rangle\} / \sqrt{2}, \\ |1,0;1^{\pm}\rangle &= \{|1^{1},0^{0};J,1\rangle \pm |1^{-1},0^{0};J,-1\rangle\} / \sqrt{2}, \\ |1,1;0^{\pm}\rangle &= \{|1^{1},1^{-1};J,0\rangle \pm |1^{-1},1^{1};J,0\rangle\} / \sqrt{2}, (5) \\ |1,1;2^{\pm}\rangle &= \{|1^{1},1^{1};J,2\rangle \pm |1^{-1},1^{-1};J,-2\rangle\} / \sqrt{2}, \end{aligned}$$

where the basis function $|v_4^{l_4}, v_5^{l_5}; J, l\rangle$ is the product of the wavefunctions of the two-dimensional-isotropic oscillators and the symmetric top wavefunction. The phases of the basis wavefunctions are so chosen that

$$\varrho = \delta_4 = \delta_5 = 0 \tag{6}$$

in the sense of Yamada [12].

The (0, 1) - (0, 0) Band of HC¹³CH

There are well known problems for the sign of the off-diagonal matrix elements of the linear-molecule Hamiltonian. However in the present case the sign of the q_5 constant has been uniquely determined, since we have observed also the well resolved Q-branch transitions in addition to those of the P and R branches. The selection rule for the Q-branch of the (0, 1) - (0, 0) band is f-e, and for the P and R branches e-e. Thus we were able to determine the symmetry and the energy of both of the l-doubling components in the (0, 1) state simultaneously. The analysis of the present data leads to a unique conclusion of positive q_5 .

The constants obtained by the least-squares analysis are listed in Table 1. The observed transition wave numbers are listed in Table 2.

Table 1. Spectroscopic parameters of $HC^{13}CH$ obtained in the present study ^a.

| Constant | Ground state | $v_5 = 1$ | | | |
|-----------------------|----------------|-----------------|--|--|--|
| G_v/cm^{-1} | | 729.378362(67) | | | |
| $B_{\rm n}/{\rm MHz}$ | 34 429.954(67) | 34 489.783 (72) | | | |
| $D_{\rm n}/{\rm kHz}$ | 46.646 (48) | 47.289 (77) | | | |
| H_v/Hz | , , | -0.027(33) | | | |
| $q_{\rm p}/{\rm MHz}$ | | 134.386(13) | | | |
| q_{Jv}/kHz | | -1.090(15) | | | |

^a Numbers in parentheses are uncertainties in one standard deviation in units of the last digit quoted.

The (1, 1) - (1, 0) Band of HCCH

The signs of the off-diagonal constants should be handled carefully in this case. Since the normal species has a center of symmetry, the intensity alternation due to the spin statistics supplies unambiguous information for the symmetry of the energy levels as listed in Table 3. The symmetry combined with the transition frequencies allowed only one choice for the signs of q_4 of the (1,0) state and r_{45} of the (1,1) state: positive q_4 and negative r_{45} . From the transition frequencies the signs of the constants q_4 and q_5 of the (1,1) state are only determinable with the assumption that the constants do not change much for the various vibrational states.

As we can see from the energy matrix of the (1, 1) state in the symmetrized basis, which is by neglecting the higher order off-diagonal terms

$$|(1,1)^{0+}\rangle \begin{pmatrix} E_{00} + r_{45} & (q_4 + q_5)f & 0 & 0\\ |(1,1)^{2+}\rangle & E_{22} & 0 & 0\\ |(1,1)^{0-}\rangle & (\text{sym.}) & E_{00} - r_{45} & (q_5 - q_4)f \\ |(1,1)^{2-}\rangle & E_{22} & 0 & 0 \end{vmatrix}$$
(6)

where E_{ii} are the matrix elements of the diagonal operator \hat{h}_{d} and

$$f = (1/2) \sqrt{J(J+1)[J(J+1)-2]},$$
 (7)

we can determine the absolute values of the sum and difference of the two *l*-type doubling constants from the energy analysis. However, as discussed by Di Lauro and Mills [13] for the Coriolis interaction, we can also determine the signs of the off-diagonal matrix elements from the intensity analysis. The sign information is carried by the eigenfunction and is revealed in the line intensity.

Table 2. Observed line positions of HC¹³CH in the v_5 band in cm⁻¹.

| J | P | | Q | | R | | |
|----------------------------|---------------------------------------------------------------|-------------------------------|----------------------------------------------------------------------------|----------------------------------|---------------------------------------------------------------|-------------------------------|--|
| | observed | obs calc. | observed | obs calc. | observed | obs calc. | |
| 1 2 3 4 5 | 723.63317 721.33570 719.03715 716.73915 714.44084 | -46 -16 -57 -8 | 728.23669 728.25363 728.27902 728.31292 728.35532 728.40614 | 30 28 24 23 25 22 | 735.11575 737.41051 739.70408 741.99825 744.29037 | 16 18 -37 36 -24 | |
| 7 8 9 10 | 712.14096 709.84216 707.54270 705.24336 | -46 2 1 27 | 728.46549 728.53333 728.60876 728.69360 | 26 34 -44 -24 | 746.58226 748.87394 751.16373 753.45338 | -34 15 -43 -28 | |
| 11 12 13 14 15 | 702.94317 700.64398 698.34396 696.04392 693.74388 | -19 42 24 6 -16 | 728.78697 729.11634 | 6 -24 | 755.74209 758.02981 760.31663 762.60260 764.88681 | -18 -12 1 31 -9 | |
| 16 17 18 19 20 | 691.44465 689.14443 686.84503 684.54542 682.24655 | 36 -20 -9 -36 -10 | 729.52206 729.67363 729.83289 730.00172 | 41 27 -49 2 | 767.17023 769.45288 771.73392 774.01426 776.29302 | -19 7 -10 25 26 | |
| 21 22 23 24 25 | 679.94746 677.64903 675.35118 673.05306 670.75545 | -29 -10 34 19 15 | 730.17815 730.36335 730.55635 730.75720 730.96684 | -15 20 12 -32 -16 | 778.57028 783.12127 785.39414 787.66654 | 7 -20 -25 28 | |
| 26 27 28 29 30 | 668.45841 666.16104 663.86491 661.56986 659.27391 | 26 -39 -30 36 -42 | 731.64443 732.13629 | 15 7 | 789.93679 792.20569 794.47254 796.73799 799.00221 | 15 21 -19 -38 -13 | |
| 31 32 33 | 656.97980 654.68601 | 6 23 | 732.39431 732.66010 732.93420 | $-13 \\ 3$ | 801.26444 803.52537 | -16 27 | |

Table 3. Symmetry and nuclear spin statistics.

| | | | J even | g_I | J odd | g_I |
|------------------|---------------|---|--------|-------|-------|-------|
| Σ_u^+ | $(1, 1)^{0+}$ | e | + a | 3 | -s | 1 |
| Σ_u^- | $(1, 1)^{0}$ | f | -s | 1 | +a | 3 |
| Δ_{u}^{+} | $(1, 1)^{2+}$ | e | +a | 3 | -s | 1 |
| Δ_{u}^{-} | $(1, 1)^{2}$ | f | -s | 1 | +a | 3 |
| Π_g^- | $(1,0)^{1+}$ | f | -a | 3 | +s | 1 |
| Π_g^+ | $(1,0)^{1}$ | e | + s | 1 | -a | 3 |

Figure 3 shows the Boltzmann plot for the observed transitions using the correct perturbed wavefunctions compared with that using unperturbed wavefunctions and that using wavefunctions calculated with improper signs of q_4 and q_5 . The Boltzmann plot is a diagram showing the energy dependence of the

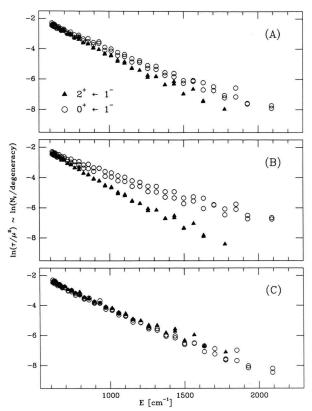


Fig. 3. Boltzmann-plot for P- and R-transitions to (upper) substates $l=0^+$ and $l=2^+$ using (A) the unperturbed wavefunction, (B) an incorrect wavefunction (q_4 and q_5 negative), and (C) the true wavefunction.

Table 4. Spectroscopic parameters of HCCH obtained in the present study ^a.

| Constant | $(v_4, v_5) = (1, 0)$ | $(v_4, v_5) = (1, 1)$ |
|------------------------|-----------------------|-----------------------|
| G_v/cm^{-1} | 612.871 в | 1 340.916082(29) |
| x_{L45}/MHz | | 198 006.1 (10) |
| B_v/MHz | 35 313.548 (32) | 35 383.795 (34) |
| d_{II}/MHz | | -3.3906(47) |
| D_{v}/kHz | 49.641 (23) | 50.372(22) |
| q_4/MHz | 156.827(13) | 159.72(11) |
| q_{J4}/kHz | -1.213(35) | -1.280(66) |
| q_{JJ4}/Hz | 0.026(23) | , |
| q_5/MHz | | 143.377(55) |
| q_{J5}/kHz | | -1.131(39) |
| r_{45}/MHz | | $-187\ 033.3(13)$ |
| r_I/MHz | | 5.8696(79) |
| r_{II}/kHz | | -0.1458(77) |

^a Numbers in parentheses are uncertainties in one standard deviation in units of the last digit quoted.

logarithm of the population obtained from the observed line intensities and the calculated line strength. If the line strengths based on the wavefunctions of the lower and upper states are correct, and if the distribution is boltzmannian, the diagram shows a single straight line, the slope of which is proportional to $(kT)^{-1}$, where T is the thermodynamical temperature of the sample during measurement. Figure 3 (A) shows that the J-dependent intensity anomalies are not taken care of by the normal Hönl-London type intensity expression: the temperature obtained from the 2^+-1^- band is apparently lower than that from the 0^+-1^- band. This effect is caused by the reduction of the intensity of the former band and enhancement of

Table 5. Observed line positions of HCCH in the $v_4 + v_5 - v_4$ band in cm⁻¹: transitions from $l=1^+$ to l=0 substate*.

| J | P | | Q | | R | | |
|----------------------------|---------------------------------------------------------------|---------------------------------------------------------------------------------------------------|---------------------------------------------------------------|------------------------------------------------------------------------------------------------------|---------------------------------------------------------------|------------------------------------------------------------------------------------------------------|--|
| | observed | obs | observed | obs calc. | observed | obs calc. | |
| 1 2 3 4 5 | 726.49586 724.13371 721.77143 719.40721 717.04279 | -5 -20 39 -15 -9 | | | 733.57657 735.93429 738.29195 740.64792 743.00225 | 24 -18 40 41 -7 | |
| 6 7 8 9 | 714.67724 712.31143 709.94537 707.57810 705.20958 | $ \begin{array}{r} -41 \\ -28 \\ 27 \\ 26 \\ -39 \end{array} $ | 716.36479 716.35886 716.34959 | -13 40 -35 | 745.35587 747.70793 750.05938 752.40935 754.75789 | $ \begin{array}{r} -6 \\ -36 \\ 2 \\ 26 \\ 46 \end{array} $ | |
| 11 12 13 14 15 | 702.84159 700.47224 698.10341 695.73322 693.36256 | $ \begin{array}{r} 6 \\ -30 \\ 37 \\ 17 \\ -5 \end{array} $ | 716.33890 716.32542 716.30794 716.28681 716.26079 | -6 37 20 33 9 | 757.10412 759.44991 761.79351 764.13586 766.47615 | $ \begin{array}{r} -20 \\ 17 \\ -10 \\ -3 \\ -38 \end{array} $ | |
| 16 17 18 19 20 | 690.99133 688.62047 686.24907 683.87712 681.50454 | $ \begin{array}{r} -41 \\ -1 \\ 23 \\ 26 \\ -2 \end{array} $ | 716.22956 716.19362 716.15004 716.10025 716.04215 | $ \begin{array}{r} -25 \\ 41 \\ -18 \\ 5 \\ -33 \end{array} $ | 768.81525 771.15235 773.48840 775.82165 778.15311 | -21 -29 39 14 | |
| 21 22 23 24 25 | 679.13222 676.75925 674.38646 672.01220 669.63892 | 28 19 54 -34 -2 | 715.97644 715.90099 715.81636 715.72145 715.61495 | $ \begin{array}{r} 7 \\ -22 \\ 5 \\ 42 \\ 20 \end{array} $ | 780.48271 782.81062 785.13593 787.45877 789.78001 | 3 40 28 -13 | |
| 26 27 28 29 30 | 667.26507 664.89060 662.51692 660.14269 657.76847 | $ \begin{array}{r} -5 \\ -53 \\ -3 \\ 7 \\ 35 \end{array} $ | 715.49655 715.36682 715.22426 714.89854 | $ \begin{array}{r} -33 \\ -2 \\ \hline 13 \\ -33 \end{array} $ | 792.09887 794.41453 796.72870 799.04055 801.34882 | $ \begin{array}{r} 24 \\ -44 \\ -16 \\ 32 \\ -21 \end{array} $ | |
| 32 34 | 653.01880 | 8 | | | 805.95874 810.55679 | 17 - 7 | |

^{*} In this table and following tables, parity of upper state is determined by the selection rules: e-e and f-f for P- and R-branches and e-f for Q-branches.

^b K. F. Palmer, M. E. Mickelson, and K. N. Rao, J. Mol. Spectrosc. **44**, 131 (1972).

Table 6. Observed line positions of HCCH in the $v_4 + v_5 - v_4$ band in cm⁻¹: transitions from l=1 to l=0 substate.

Table 7. Observed line positions of HCCH in the $v_4 + v_5 - v_4$ band in cm⁻¹: transitions from $l = 1^+$ to l = 2 substate.

| J | P | | Q | | R | | J | P | | Q | | R | |
|----------------------------|---------------------------------------------------------------|---------------------------------------------------------------------------------------------------|---------------------------------------------------------------|---------------------------------------------------------------------------------------------------|---------------------------------------------------------------|---------------------------------------------------------------------------------------------------|----------------------------|---------------------------------------------------------------|----------------------------------------------------------------------------------------------------|-------------------------------------|------------------|---------------------------------------------------------------|--------------------------------|
| | observed | obs | observed | obs calc. | observed | obs calc. | | observed | obs calc. | observed | obs | observed | obs calc. |
| 1 2 3 4 5 | 714.02846 711.68881 709.35862 707.03885 704.72957 | -39 25 2 -8 10 | 728.86641 728.91394 728.95215 | | 721.11141 723.49320 725.88367 728.28430 730.69495 | -17 37 -35 -61 -32 | 1 2 3 4 5 | 724.02073 721.65598 719.28967 | $-31 \\ 7 \\ 17$ | 731.10438 731.10002 731.09502 | 16 -8 23 | 735.82593 738.18307 740.53801 742.89167 745.24321 | -40 4 -16 -6 -47 |
| 6 7 8 9 10 | 702.43005 700.14037 697.86076 695.59059 693.32923 | $ \begin{array}{r} -3 \\ -21 \\ 0 \\ 24 \\ 17 \end{array} $ | 729.05658 729.19916 | | 733.11448 735.54308 737.98023 740.42528 732.87698 | -31 -7 29 52 -14 | 6 7 8 9 10 | 716.92187 714.55332 712.18306 709.81200 707.44011 | 0 25 -7 -11 7 | 731.07374 731.05757 | 6 -30 | 747.59355 749.94274 752.28902 754.63420 756.97740 | -41 18 -41 -34 -45 |
| 11 12 13 14 15 | 691.07697 688.83235 686.59580 684.36776 682.14589 | 44 -2 -37 32 19 | 729.48441 729.59758 729.72116 729.99495 | $-\frac{39}{17}$ -17 -17 | 745.33667 747.80213 750.27477 752.75161 755.23320 | $ \begin{array}{r} 13 \\ -31 \\ 49 \\ 20 \\ 1 \end{array} $ | 11 12 13 14 15 | 705.06732 702.69269 700.31796 697.94221 695.56541 | 35 -27 -9 -8 -31 | | | 759.31955 761.65891 763.99641 766.33295 768.66675 | 21 -7 -31 39 31 |
| 16 17 18 19 20 | 679.93022 677.72116 675.51660 673.31769 671.12145 | -17 20 -19 42 -32 | 730.14615 730.30678 730.47618 730.65516 730.84282 | $ \begin{array}{r} -7 \\ 18 \\ -5 \\ 9 \\ -26 \end{array} $ | 757.71928 760.20777 762.69933 765.19283 767.68714 | $ \begin{array}{r} 33 \\ -22 \\ -24 \\ -16 \\ -36 \end{array} $ | 16 17 18 19 20 | 693.18840 690.81022 688.43170 686.05281 683.67265 | $ \begin{array}{r} -1 \\ -18 \\ -5 \\ 32 \\ -5 \end{array} $ | 731.10960 | 26 | 770.99876 773.32806 775.65654 777.98240 780.30563 | 40 -21 38 40 -13 |
| 21 22 23 24 25 | 668.92935 666.74013 664.55271 662.36674 660.18175 | $ \begin{array}{r} -27 \\ -6 \\ -8 \\ -6 \\ 18 \end{array} $ | 731.46148 731.68614 731.91908 | $-33 \\ 0 \\ -36$ | 770.18199 772.67721 775.16980 777.66216 780.15140 | $ \begin{array}{r} -38 \\ 33 \\ -51 \\ 20 \\ 20 \end{array} $ | 21 22 23 24 25 | 681.29205 678.91181 676.53102 674.14956 671.76739 | $ \begin{array}{r} -38 \\ 8 \\ 36 \\ 29 \\ -26 \end{array} $ | 731.14140 731.28496 731.35081 | -17 -26 -9 | 782.62714 784.94704 787.26435 789.57917 791.89241 | -28 8 -1 -43 -25 |
| 26 27 28 29 30 | 657.99672 655.81106 653.62452 651.43673 649.24629 | 22 5 -4 9 -52 | 732.16166 732.41259 732.67248 732.94146 | $ \begin{array}{r} -1 \\ -17 \\ -20 \\ 9 \end{array} $ | 782.63708 785.11982 787.59811 790.07239 792.54099 | $ \begin{array}{r} -30 \\ -12 \\ -24 \\ 27 \\ 17 \end{array} $ | 26 27 28 29 30 | 669.38551 667.00372 664.62197 662.23940 659.85770 | -31 -15 13 -41 -14 | 731.42615 731.60943 | -32 -2 | 794.20387 796.51218 798.81802 801.12299 803.42466 | 36 2 -56 24 0 |
| 31 32 33 34 35 | 647.05492 644.86018 642.66215 638.25651 | 27 34 11 -14 | 733.50491 733.79935 734.10232 734.41464 | 9 -11 -32 36 | 795.00426 797.46173 799.91288 804.79693 | 19 17 -13 -9 | 31 32 34 36 | 655.09446 | 11 | 731.97022 732.11549 732.44294 | -14 32 -14 | 805.72508 808.02162 812.60943 817.18812 | 77 -5 -6 5 |

the latter by the mixing of the wavefunctions due to the l-type resonance. If we correct this effect, we obtain Fig. 3 (C): both bands show a consistent temperature. If we use incorrect sign of the q's, the inconsistence in the temperature increases: this is shown in Figure 3 (B).

By using the Boltzmann plot for all possible choices we have determined uniquely the value (including its sign) of q_4 and q_5 in the (1, 1) vibrational states. The constants thus determined by a least-squares analysis are listed in Table 4. The measured transitions are contained in Tables 5-8.

IV. Conclusion

We report here improved spectroscopic constants of $HC^{13}CH$ in the ground and $v_5=1$ states, and those of HCCH in the $v_4=1$ and $(v_4,v_5)=(1,1)$ states. The present results are consistent with values quoted in the literature, especially they are in a good agreement with Hietanen and Kauppinen [3]. The present work has been carried out with slightly better resolution and consequently better precision.

The line intensities also supply important information about the molecular constants. In the present

Table 8. Observed line positions of HCCH in the $v_4 + v_5 - v_4$ band in cm⁻¹: transitions from l=1 to l=2 substate.

| J | P | | Q | | R | | |
|----------------------------|---------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------|---------------------------------------------------------------------------------------------------|---------------------------------------------------------------|------------------------------|--|
| | observed | obs calc. | observed | obs | observed | obs | |
| 1 2 3 4 5 | 724.08406 721.76111 719.44677 | 21 39 -24 | 731.13519 731.16273 731.19822 731.24421 | -38 7 -57 26 | 735.83709 738.21457 740.60173 742.99762 745.40359 | 26 -4 18 -15 | |
| 6 7 8 9 | 717.14249 714.84898 712.56510 710.29074 708.02874 | -45 23 39 -43 26 | 731.29845 731.36142 731.43325 731.51496 731.60537 | 32 7 -34 11 24 | 747.81885 750.24402 752.67969 755.12557 757.58227 | 10 5 33 31 23 | |
| 11 12 13 14 15 | 705.77726 703.53676 701.30943 699.09480 696.89332 | 22 -53 -29 -6 7 | 731.70477 731.81304 731.93024 732.19203 | 33 28 15 | 760.05027 762.52996 765.02221 767.52616 770.04411 | 18 10 39 -32 -27 | |
| 16 17 18 19 20 | 694.70538 692.53205 690.37380 688.23182 686.10540 | $ \begin{array}{r} -9 \\ -10 \\ -12 \\ \hline 37 \\ -1 \end{array} $ | 732.33584 732.48944 732.65195 733.00366 | $ \begin{array}{r} -30 \\ -6 \\ 9 \end{array} $ | 772.57647 775.12186 777.68331 780.26020 782.85296 | 40 -29 10 35 26 | |
| 21 22 23 24 25 | 683.99674 681.90521 679.83261 677.77956 675.74618 | 25 -18 -17 21 42 | 733.19282 733.39163 733.59883 733.81476 734.03969 | $ \begin{array}{r} -8 \\ 40 \\ 28 \\ -9 \\ -44 \end{array} $ | 785.46192 788.08916 790.73420 793.39830 796.08112 | -44 -28 -30 19 | |
| 26 27 28 29 30 | 673.73213 671.74080 667.82238 | -51 20 42 | 734.27433 734.51774 734.77012 735.03157 735.30108 | $ \begin{array}{r} -8 \\ 9 \\ 24 \\ 48 \\ -21 \end{array} $ | 798.78303 801.50530 804.24768 807.01078 | -22 -48 | |
| 31 32 33 | | | 735.58013 735.86879 736.16542 | -33 18 -32 | 812.60166 | 39 | |

study it is shown that one can determine the sign of the *l*-type resonance interaction constants by using the intensity anomaly. In the other words, we have found that the l-type resonance interaction produces an unignorable amount of intensity change. Since this resonance is a common interaction for linear molecules, i.e. an inherent interaction and not accidental, we would like to stress that the l-type resonance effect has to be always taken into account in the intensity analysis of a linear molecule.

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